

Ant Colony Meta-heuristic

■ Procedure AntMetaHeuristic

- Set parameters, initial pheromone levels
- **While** (termination condition not met) **do**
 - Construct Ants' Solutions
 - Evaluate Solutions
 - Update Pheromones (according to soln goodness)

□ **End**

■ End

Ant Colony System

- An iterative optimization method, extension of the AntMetaheuristic
- Was shown to be competitive with state-of-the-art algorithms in solving the TSP
- When making a choice ants consider:
 - Static (heuristic) distance information
 - Dynamic (pheromone level) experience

Heuristic Computation

- Ants make decisions maximizing

$$\text{Heuristic} = \text{pheromone} * (1 / \text{distance})$$

$$\text{Nearness(Blagoevgrad, Sofia)} = 1 / 100 = 0.01$$

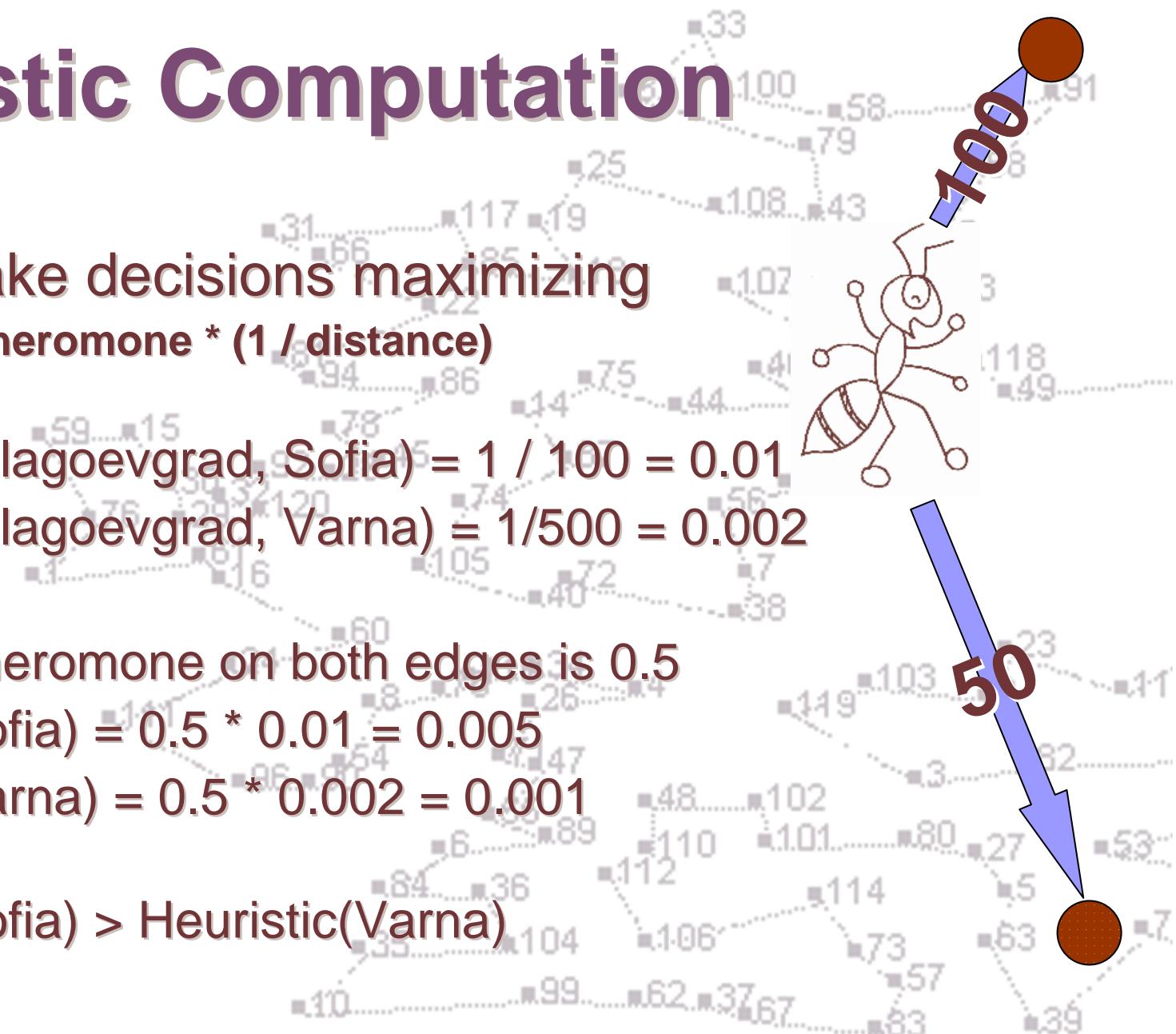
$$\text{Nearness(Blagoevgrad, Varna)} = 1/500 = 0.002$$

Suppose pheromone on both edges is 0.5

$$\text{Heuristic(Sofia)} = 0.5 * 0.01 = 0.005$$

$$\text{Heuristic(Varna)} = 0.5 * 0.002 = 0.001$$

$$\text{Heuristic(Sofia)} > \text{Heuristic(Varna)}$$



Solution Construction

Ant is at city r .

The probability of choosing next city to be s depends on:

1. The heuristic value (nearness * pheromone)
2. The value of a random number $q \sim (0, 1)$ and a threshold $q_0 = 0.9$

If $q < q_0$

$r = \text{max heuristic city (exploitation)}$

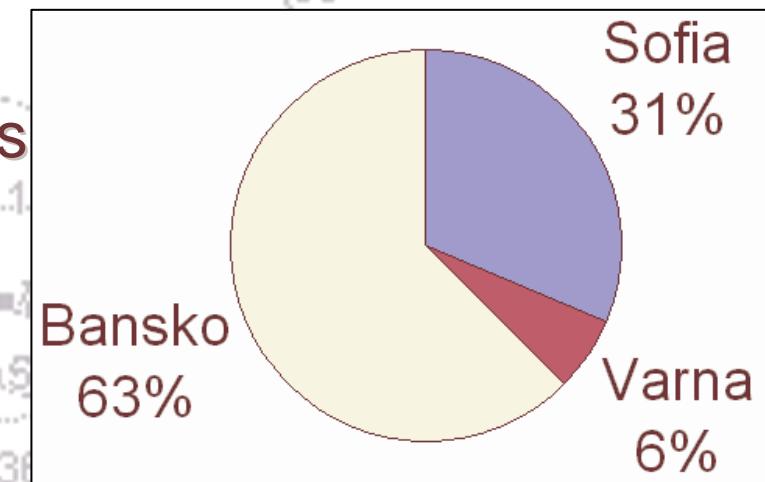
Else

$r = \text{random proportional choice from non-visited cities (exploration)}$

Exploration Mode City Choice

| | Pheromone | Distance | Nearness | Heuristic | Ratio |
|--------|-----------|----------|----------|-----------|--------|
| Sofia | 0.1 | 100 | 0.01 | 0.001 | 31.25% |
| Varna | 0.1 | 500 | 0.002 | 0.0002 | 6.25% |
| Bansko | 0.1 | 50 | 0.02 | 0.002 | 62.5% |

1. Calculate **Heuristic** for all cities
2. Normalize **Heuristic** values
3. Generate a number (0,360)
and select the corresponding city



Pheromone Update Rules

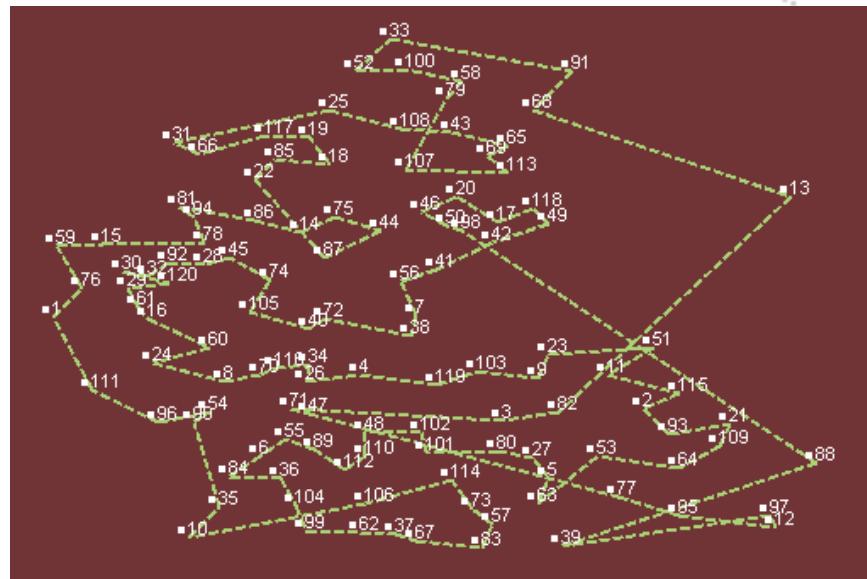
- Elitist approach – only the best tour so far is used to globally update pheromone
 - Favors exploitation of the best tour so far
- Local pheromone update – weakens the pheromone trail of an edge, once an ant has traversed it
 - Prevents pheromone trail value explosion
 - Favors exploration and prevents premature convergence

Recap

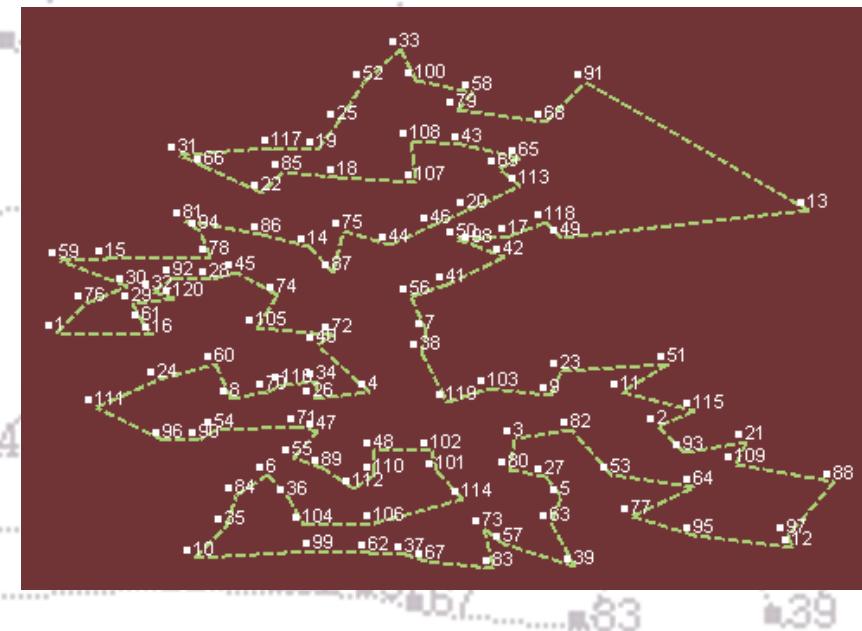
- Traveling Salesman Problem (TSP)
- Ant Colonies in Nature and Optimization
- Ant Colony Meta-Heuristic Overview
- Ant Colony System
- Test Results
- Applications
- Summary

Initial and Final Tours – gr120

Initial Tour

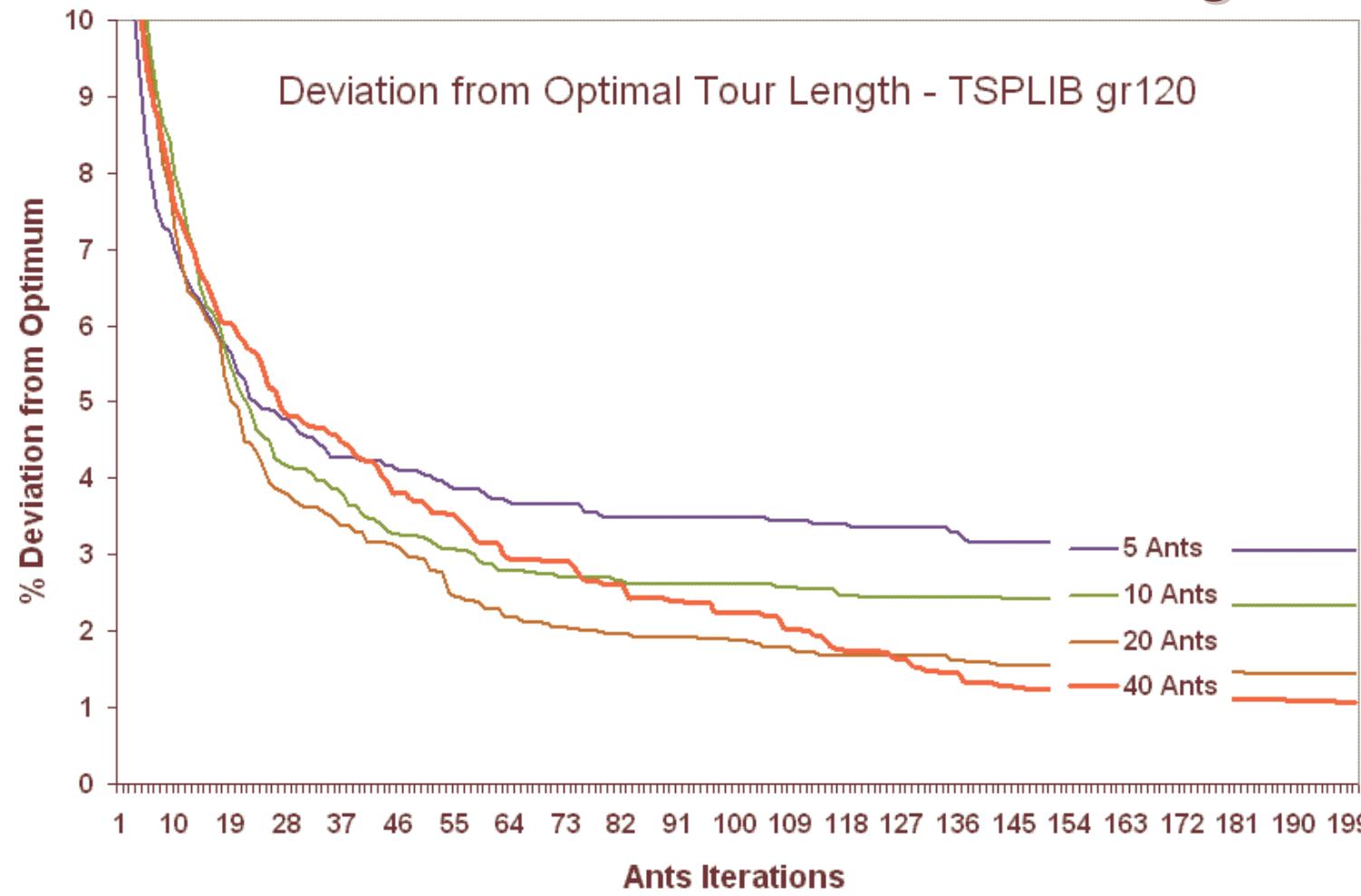


Final Tour – 200 iterations, 40 ants



Test Results

Different number of ants - TSPLIB gr120



Test Results

■ Different number of ants - TSPLIB pr1002

