

## ANISOTROPIC PARABOLIC EQUATIONS WITH VARIABLE NONLINEARITY

S. ANTONTSEV AND S. SHMAREV

*Abstract*

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We study the Dirichlet problem for a class of nonlinear parabolic equations with nonstandard anisotropic growth conditions. Equations of this class generalize the evolutionary  $p(x, t)$ -Laplacian. We prove theorems of existence and uniqueness of weak solutions in suitable Orlicz-Sobolev spaces, derive global and local in time  $L^\infty$  bounds for the weak solutions.

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