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## INTERMEDIARIES IN BREDON (CO)HOMOLOGY AND CLASSIFYING SPACES

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**Abstract:** For certain contractible *G*-CW-complexes and  $\mathfrak{F}$  a family of subgroups of *G*, we construct a spectral sequence converging to the  $\mathfrak{F}$ -Bredon cohomology of *G* with  $\mathbb{E}_1$ -terms given by the  $\mathfrak{F}$ -Bredon cohomology of the stabilizer subgroups. As applications, we obtain several corollaries concerning the cohomological and geometric dimensions of the classifying space  $E_{\mathfrak{F}}G$ . We also introduce, for any subgroup closed class of groups  $\mathfrak{F}$ , a hierarchically defined class of groups and show that if a group *G* is in this class, then *G* has finite  $\mathfrak{F} \cap G$ -Bredon (co)homological dimension if and only if *G* has jump  $\mathfrak{F} \cap G$ -Bredon (co)homology.

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