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## DEGREE OF THE FIRST INTEGRAL OF A PENCIL IN $\mathbb{P}^2$ DEFINED BY LINS NETO

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**Abstract:** Let  $\mathcal{P}_4$  be the linear family of foliations of degree 4 in  $\mathbb{P}^2$  introduced by A. Lins Neto, whose set of parameter with first integral  $I_p(\mathcal{P}_4)$  is dense and countable. In this work, we will compute explicitly the degree of the rational first integral of the foliations in this linear family, as a function of the parameter.

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Key words: Poincaré problem, pencil of foliations, first integral.