# DEGREE OF THE FIRST INTEGRAL OF A PENCIL IN $\mathbb{P}^{2}$ DEFINED BY LINS NETO 

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#### Abstract

Let $\mathcal{P}_{4}$ be the linear family of foliations of degree 4 in $\mathbb{P}^{2}$ introduced by A. Lins Neto, whose set of parameter with first integral $I_{p}\left(\mathcal{P}_{4}\right)$ is dense and countable. In this work, we will compute explicitly the degree of the rational first integral of the foliations in this linear family, as a function of the parameter.


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Key words: Poincaré problem, pencil of foliations, first integral.

