NON-EXISTENCE OF MULTI-LINE BESICOVITCH SETS

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Abstract: If a compact set $K \subset \mathbb{R}^2$ contains a positive-dimensional family of line-segments in every direction, then $K$ has positive measure.

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