

SUMMATION OF COEFFICIENTS OF POLYNOMIALS ON ℓ_p SPACES

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Abstract: We investigate the summability of the coefficients of m -homogeneous polynomials and m -linear mappings defined on ℓ_p spaces. In our research we obtain results on the summability of the coefficients of m -linear mappings defined on $\ell_{p_1} \times \cdots \times \ell_{p_m}$. The first results in this respect go back to Littlewood [17] and Bohnenblust and Hille [6] for bilinear and m -linear forms on c_0 , and Hardy and Littlewood [15] and Praciano-Pereira [20] for bilinear and m -linear forms on arbitrary ℓ_p spaces. Our results recover and in some case complete these old results through a general approach on vector valued m -linear mappings.

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