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Ant colony Optimization Algorithms : Introduction and Beyond

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Ant Colony Optimization

What is Ant Colony Optimization?

- Probabilistic technique.
- Searching for optimal path in the graph based on behaviour of ants seeking a path between their colony and source of food.
- Meta-heuristic optimization

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Ant Colony Opt	imization				
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Overview of the Concept

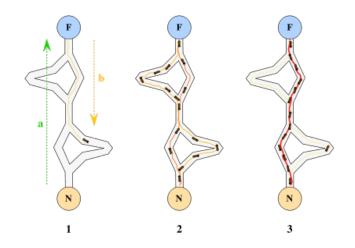
- Ants navigate from nest to food source. Ants are blind!
- Shortest path is discovered via pheromone trails.
- Each ant moves at random
- Pheromone is deposited on path
- More pheromone on path increases probability of path being followed

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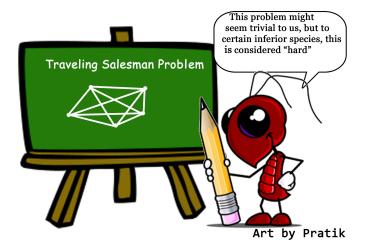
Ant Colony Optimization



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Ant Colony Optimization



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Overview of the System

- Virtual trail accumulated on path segments
- Path selected at random based on amount of "trail" present on possible paths from starting node

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Overview of the System

- Virtual trail accumulated on path segments
- Path selected at random based on amount of "trail" present on possible paths from starting node
- Ant reaches next node, selects next path
- Continues until reaches starting node

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Overview of the System

- Virtual trail accumulated on path segments
- Path selected at random based on amount of "trail" present on possible paths from starting node
- Ant reaches next node, selects next path
- Continues until reaches starting node
- Finished tour is a solution.
- Tour is analyzed for optimality

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Meta-heuristic C	Optimization				
Meta-he	uristic				

 Heuristic method for solving a very general class of computational problems by combining user-given heuristics in the hope of obtaining a more efficient procedure.

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Meta-heuristic C	Optimization				
Meta-he	uristic				

- Heuristic method for solving a very general class of computational problems by combining user-given heuristics in the hope of obtaining a more efficient procedure.
- 2 ACO is meta-heuristic
- Soft computing technique for solving hard discrete optimization problems

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History

History



- Ant System was developed by Marco Dorigo (Italy) in his PhD thesis in 1992.
- Max-Min Ant System developed by Hoos and Stützle in 1996
- Ant Colony was developed by Gambardella Dorigo in 1997

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The ACO Metaheuristic

The ACO Meta-heuristic

ACO

Set Parameters, Initialize pheromone trails

SCHEDULE ACTIVITIES

- Construct Ant Solutions
- 2 Daemon Actions (optional)
- Opdate Pheromones

Virtual trail accumulated on path segments

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The ACO Metaheuristic

ACO - Construct Ant Solutions



ACO - Construct Ant Solutions

An ant will move from node i to node j with probability

$$oldsymbol{p}_{i,j} = rac{(au_{i,j}^lpha)(\eta_{i,j}^eta)}{\sum (au_{i,j}^lpha)(\eta_{i,j}^eta)}$$

where

 $\tau_{i,j}$ is the amount of pheromone on edge i, j α is a parameter to control the influence of $\tau_{i,j}$ $\eta_{i,j}$ is the desirability of edge i, j (typically $1/d_{i,j}$) β is a parameter to control the influence of $\eta_{i,j}$

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The ACO Metal	neuristic				

ACO - Pheromone Update

ACO - Pheromone Update

Amount of pheromone is updated according to the equation

$$\tau_{i,j} = (1 - \rho)\tau_{i,j} + \Delta \tau_{i,j}$$

where

 $\tau_{i,j}$ is the amount of pheromone on a given edge i, j

 ρ is the rate of pheromone evaporation

 $\Delta \tau_{i,j}$ is the amount of pheromone deposited, typically given by

$$\Delta \tau_{i,j}^{k} = \begin{cases} 1/L_{k} & \text{if ant } k \text{ travels on edge } i, \\ 0 & \text{otherwise} \end{cases}$$

where L_k is the cost of the k^{th} ant's tour (typically length).

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Main ACO Algo	rithms				
ACO					

- Many special cases of the ACO metaheuristic have been proposed.
- The three most successful ones are: Ant System, Ant Colony System (ACS), and MAX-MIN Ant System (MMAS).
- For illustration, example problem used is Travelling Salesman Problem.

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Ant System					
	nt System				

ACO - Ant System

- First ACO algorithm to be proposed (1992)
- Pheromone values are updated by all the ants that have completed the tour.

$$au_{ij} \leftarrow (1-
ho) \cdot au_{ij} + \sum_{k=1}^m \Delta au_{ij}^k$$

where

 ρ is the evaporation rate

m is the number of ants

 $\Delta \tau_{ij}^k$ is pheromone quantity laid on edge (i, j) by the k^{th} ant

$$\Delta \tau_{i,j}^{k} = \begin{cases} 1/L_{k} & \text{if ant } k \text{ travels on edge } i, j \\ 0 & \text{otherwise} \end{cases}$$

where L_k is the tour length of the k^{th} ant.

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Ant Colony System

ACO - Ant Colony System

ACO - Ant Colony System

- First major improvement over Ant System
- Differences with Ant System:
 - Decision Rule Pseudorandom proportional rule
 - 2 Local Pheromone Update
 - Best only offline Pheromone Update

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Ant Colony System

ACO - Ant Colony System



ACO - Ant Colony System

- Ants in ACS use the pseudorandom proportional rule
- Probability for an ant to move from city *i* to city *j* depends on a random variable *q* uniformly distributed over [0, 1], and a parameter *q*₀.
- If $q \leq q_0$, then, among the feasible components, the component that maximizes the product $\tau_{il}\eta_{il}^{\beta}$ is chosen, otherwise the same equation as in Ant System is used.
- This rule favours exploitation of pheromone information

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Ant Colony System

ACO - Ant Colony System

ACO - Ant Colony System

- Diversifying component against exploitation: local pheromone update.
- The local pheromone update is performed by all ants after each step.
- Each ant applies it only to the last edge traversed:

$$\tau_{ij} = (\mathbf{1} - \varphi) \cdot \tau_{ij} + \varphi \cdot \tau_0$$

where

 $\varphi \in (0, 1]$ is the pheromone decay coefficient τ_0 is the initial value of the pheromone (value kept small *Why?*)

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ACO - Ant Colony System

- Best only offline pheromone update after construction
- Offline pheromone update equation

$$au_{ij} \leftarrow (1 - \rho) \cdot au_{ij} + \rho \cdot \Delta au_{ij}^{best}$$

where

$$au_{ij}^{best} = egin{cases} 1/L_{best} & ext{if best ant } k ext{ travels on edge } i, j \ 0 & ext{otherwise} \end{cases}$$

• *L*_{best} can be set to the length of the best tour found in the current iteration or the best solution found since the start of the algorithm.

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MAX-MIN Ant System

ACO - MAX-MIN Ant System

ACO - MAX-MIN Ant System

Differences with Ant System:

- Best only offline Pheromone Update
- 2 Min and Max values of the pheromone are explicitly limited
 - τ_{ij} is constrained between τ_{min} and τ_{max} (explicitly set by algorithm designer).
 - After pheromone update, τ_{ij} is set to τ_{max} if $\tau_{ij} > \tau_{max}$ and to τ_{min} if $\tau_{ij} < \tau_{min}$

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- Routing in telecommunication networks
- Traveling Salesman
- Graph Coloring
- Scheduling
- Constraint Satisfaction

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• Inherent parallelism

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Advantages

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- Inherent parallelism
- Positive Feedback accounts for rapid discovery of good solutions

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Advantages

Advantages of ACO

- Inherent parallelism
- Positive Feedback accounts for rapid discovery of good solutions
- Efficient for Traveling Salesman Problem and similar problems

Advantages

Advantages of ACO

- Inherent parallelism
- Positive Feedback accounts for rapid discovery of good solutions
- Efficient for Traveling Salesman Problem and similar problems
- Can be used in dynamic applications (adapts to changes such as new distances, etc)

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Disadvanatges								
Disadva	Disadvantages of ACO							



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• Theoretical analysis is difficult

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Disadvanatges

Disadvantages of ACO

- Theoretical analysis is difficult
- Sequences of random decisions (not independent)

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Disadvanatges

Disadvantages of ACO

- Theoretical analysis is difficult
- Sequences of random decisions (not independent)
- Probability distribution changes by iteration

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Disadvantages of ACO

- Theoretical analysis is difficult
- Sequences of random decisions (not independent)
- Probability distribution changes by iteration
- Research is experimental rather than theoretical

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Disadvanatges

Disadvantages of ACO

- Theoretical analysis is difficult
- Sequences of random decisions (not independent)
- Probability distribution changes by iteration
- Research is experimental rather than theoretical
- Time to convergence uncertain (but convergence is gauranteed!)

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 Artificial Intelligence technique used to develop a new method to solve problems unsolvable since last many years

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Summa	ry				

- Artificial Intelligence technique used to develop a new method to solve problems unsolvable since last many years
- ACO is a recently proposed metaheuristic approach for solving hard combinatorial optimization problems.

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Summa	ry				

- Artificial Intelligence technique used to develop a new method to solve problems unsolvable since last many years
- ACO is a recently proposed metaheuristic approach for solving hard combinatorial optimization problems.
- Artificial ants implement a randomized construction heuristic which makes probabilistic decisions

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Summa	ry				

- Artificial Intelligence technique used to develop a new method to solve problems unsolvable since last many years
- ACO is a recently proposed metaheuristic approach for solving hard combinatorial optimization problems.
- Artificial ants implement a randomized construction heuristic which makes probabilistic decisions
- ACO shows great performance with the "ill-structured" problems like network routing



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Thank You.. Questions??