Deterministic optimization assignment

January 16, 2022

The Rosenbrock's function is:

$$f(x_1, x_2) := 100(x_2 - x_1^2)^2 + (1 - x_1)^2.$$

The exercise consists in solving the problem of minimizing f over \mathbb{R}^2 starting at the point (-1.5, -1). Is this point a good seed?

Compare the three different methods below by explaining towards which point do they converge, and how many iterations are required.

(Where) Is f convex? Are the points obtained a global minimum?

Methods to program:

- (a) the (standard plain) Steepest Descent (Gradient) Method,
- (b) the Conjugate Gradient Method, and
- (c) Levenberg–Marquardt.