

Localizing Limit Cycles: From Numeric to Analytical Results



Armengol Gasull, Héctor Giacomini and Maite Grau

Abstract This note presents the results of [4]. It deals with the problem of location and existence of limit cycles for real planar polynomial differential systems. We provide a method to construct Poincaré–Bendixson regions by using transversal curves, that enables us to prove the existence of a limit cycle that has been numerically detected. We apply our results to several known systems, like the Brusselator one or some Liénard systems, to prove the existence of the limit cycles and to locate them very precisely in the phase space. Our method, combined with some other classical tools can be applied to obtain sharp bounds for the bifurcation values of a saddle-node bifurcation of limit cycles, as we do for the Rychkov system.

1 Introduction

We consider real planar polynomial differential systems of the form

$$\dot{x} = dx/dt = P(x, y), \quad \dot{y} = dy/dt = Q(x, y), \quad (1)$$

A. Gasull (✉)

Departament de Matemàtiques, Universitat Autònoma de Barcelona,
08193 Bellaterra, Barcelona, Catalonia, Spain
e-mail: gasull@mat.uab.cat

H. Giacomini

Laboratoire de Mathématiques et Physique Théorique. C.N.R.S. UMR 7350.,
Faculté des Sciences et Techniques, Université de Tours., Parc de Grandmont,
37200 Tours, France
e-mail: Hector.Giacomini@lmpt.univ-tours.fr

M. Grau

Departament de Matemàtica, Universitat de Lleida, Avda. Jaume II, 69,
25001 Lleida, Catalonia, Spain
e-mail: mtgrau@matematica.udl.cat