Non-Existence, Uniqueness of Limit Cycles and Center Problem in a System That Includes Predator-Prey Systems and Generalized Lienard Equations

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(Submitted by: K.P. Hadeler)

Abstract

We study the number of periodic orbits of a family of planar differential equations that includes usual predator-prey systems and generalized Liénard equations. More explicitly, we give conditions for non-existence, uniqueness and hyperbolicity of periodic orbits and also for the existence of centers. The main tool used is a generalization of the Filippov transformation. We apply the results on non-existence of periodic orbits and on the existence of centers to some predator-prey systems found in the literature. The result on uniqueness is applied to some generalized Liénard equations.

Received on April 18, 1995.

AMS (MOS) 1991 Subject classifications: 34C05, 92D25.

^{*}Partially supported by the DGICYT grant number PB90-0695.

[†]Partially supported by M.E.C.-DGICYT grant number AP90-46670968.