

# Outbreak analysis of an SIS epidemic model with rewiring

David Juher · Jordi Ripoll · Joan Saldaña

Received: 16 February 2012 / Revised: 18 May 2012 / Published online: 12 June 2012  
© Springer-Verlag 2012

**Abstract** This paper is devoted to the analysis of the early dynamics of an SIS epidemic model defined on networks. The model, introduced by Gross et al. (Phys Rev Lett 96:208701, 2006), is based on the pair-approximation formalism and assumes that, at a given rewiring rate, susceptible nodes replace an infected neighbour by a new susceptible neighbour randomly selected among the pool of susceptible nodes in the population. The analysis uses a triple closure that improves the widely assumed in epidemic models defined on regular and homogeneous networks, and applies it to better understand the early epidemic spread on Poisson, exponential, and scale-free networks. Two extinction scenarios, one dominated by transmission and the other one by rewiring, are characterized by considering the limit system of the model equations close to the beginning of the epidemic. Moreover, an analytical condition for the occurrence of a bistability region is obtained.

**Keywords** Pair approximation · Network epidemic models · Rewiring · Basic reproduction number

**Mathematics Subject Classification** 92D30 (epidemiology) · 05C82 (small world graphs, complex networks) · 34C60 (qualitative investigation and simulation of models) · 90B15 (network models, stochastic)

---

D. Juher · J. Ripoll · J. Saldaña (✉)  
Departament d'Informàtica i Matemàtica Aplicada,  
Universitat de Girona, 17071 Girona, Catalonia, Spain  
e-mail: jsaldana@ima.udg.edu

D. Juher  
e-mail: juher@ima.udg.edu

J. Ripoll  
e-mail: jripoll@ima.udg.edu