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## On the central configurations of the $n$ -body problem

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### Abstract

We present a brief survey on some classes of central configurations of the  $n$ -body problem. We put special emphasis on the central configurations of the  $1 + n$ -body problem also called the coorbital satellite problem, and on the nested central configurations formed by either regular  $n$ -gons, or regular polyhedra. We also present some conjectures.

**Keywords:**  $n$ -body problem, central configurations.

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## 1 Introduction

### 1.1 The $n$ -body problem

The  $n$ -body problem consists in studying the motion of  $n$  pointlike masses, interacting among themselves through no other forces than their mutual gravitational attraction according to Newton's gravitational law.

The *equations of motion* of the  $n$ -body problem are

$$m_k \mathbf{r}''_k = \sum_{j=1, j \neq k}^n \frac{G m_j m_k}{r_{jk}^3} (\mathbf{r}_j - \mathbf{r}_k),$$

for  $k = 1, \dots, N$ , where  $G$  is the gravitational constant,  $\mathbf{r}_k \in \mathbb{R}^3$  is the position vector of the punctual mass  $m_k$  in an inertial system, and  $r_{jk}$  is the Euclidean distance between the masses  $m_j$  and  $m_k$ .

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