



Contents lists available at ScienceDirect

Bulletin des Sciences Mathématiques

www.elsevier.com/locate/bulsci



First integrals of Darboux type for a family of 3-dimensional Lotka–Volterra systems



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ARTICLE INFO

Article history:

Received 12 July 2014

Available online 24 October 2014

MSC:

34C05

34A34

34C14

Keywords:

Integrability of Darboux type

Lotka–Volterra systems

May–Leonard system

ABSTRACT

We provide all the first integrals of Darboux type for the system studied by Leach and Miritzis (2006) [7] on the classical model of competition between three species considered by May and Leonard (1975) [12].

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1. Introduction and statement of the main results

In this paper we use the Darboux theory of integrability [5] to study the existence of first integrals of Darboux type for the model used by May and Leonard [12] for studying the competition among three species. This model is

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