# Simultaneous bifurcation of limit cycles from a linear center with extra singular points ${ }^{\text {*i }}$ 

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#### Abstract

The period annuli of the planar vector field $x^{\prime}=-y F(x, y), y^{\prime}=x F(x, y)$, where the set $\{F(x, y)=0\}$ consists of $k$ different isolated points, is defined by $k+1$ concentric annuli. In this paper we perturb it with polynomials of degree $n$ and we study how many limit cycles bifurcate, up to a first order analysis, from all the period annuli simultaneously in terms of $k$ and $n$. Additionally, we prove that the associated Abelian integral is piecewise rational and, when $k=1$, the provided upper bound is reached. Finally, the case $k=2$ is also treated.


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## 1. Introduction

Let $H, f, g$ be polynomials in $x, y$ such that $\gamma_{h} \subseteq\{H(x, y)=h\}$, with $h \in\left(h_{0}, h_{1}\right)$, are simple closed curves around the point $\left(x_{0}, y_{0}\right)=\gamma_{h_{0}}$. Then the system

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