

TWO WEIGHTED INEQUALITIES FOR CONVOLUTION MAXIMAL OPERATORS

A. L. BERNARDIS* AND F. J. MARTÍN-REYES†

Abstract

Let $\varphi: \mathbb{R} \rightarrow [0, \infty)$ an integrable function such that $\varphi\chi_{(-\infty, 0)} = 0$ and φ is decreasing in $(0, \infty)$. Let $\tau_h f(x) = f(x - h)$, with $h \in \mathbb{R} \setminus \{0\}$ and $f_R(x) = \frac{1}{R}f(\frac{x}{R})$, with $R > 0$. In this paper we characterize the pair of weights (u, v) such that the operators $M_{\tau_h \varphi} f(x) = \sup_{R>0} |f| * [\tau_h \varphi]_R(x)$ are of weak type (p, p) with respect to (u, v) , $1 < p < \infty$.

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