## WEIGHTED HARDY'S INEQUALITIES FOR NEGATIVE INDICES

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Abstract \_\_\_\_

In the paper we obtain a precise characterization of Hardy type inequalities with weights for the negative indices and the indices between 0 and 1 and establish a duality between these cases.

<sup>2000</sup> Mathematics Subject Classification. 26D15, 26D10.

Key words. Hardy's inequality, weight function, negative indices, duality.

The research was partially supported by the Russian Foundation for Basic Research (Project 03–01–00017) and by the Russian Academy of Science (Project 04–3– $\Gamma$ –01–049).