DÉFORMATION LOCALISÉE DE SURFACES DE RIEMANN

Peter Haïssinsky

Abstract

Let Y be a Riemann surface with compact boundary embedded into a hyperbolic Riemann surface of finite type X. It is proved that the space of deformations $\mathcal D$ of Y into X is an open subset of the Teichmüller space $\mathcal T(X)$ of X. Furthermore, $\mathcal D$ has compact closure if and only if Y is simply connected or isomorphic to a punctured disk, and $\mathcal D=\mathcal T(X)$ if and only if the components of $X\setminus Y$ are all disks or punctured disks.

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