# HYBRID BOUNDS FOR TWISTS OF $G L(3)$ L-FUNCTIONS 

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#### Abstract

Let $\pi$ be a Hecke-Maass cusp form for $S L(3, \mathbb{Z})$ and $\chi=\chi_{1} \chi_{2}$ a Dirichlet character with $\chi_{i}$ primitive modulo $M_{i}$. Suppose that $M_{1}, M_{2}$ are primes such that $\max \left\{(M|t|)^{1 / 3+2 \delta / 3}, M^{2 / 5}|t|^{-9 / 20}, M^{1 / 2+2 \delta}|t|^{-3 / 4+2 \delta}\right\}(M|t|)^{\varepsilon}<M_{1}<\min \left\{(M|t|)^{2 / 5}\right.$, $\left.(M|t|)^{1 / 2-8 \delta}\right\}(M|t|)^{-\varepsilon}$ for any $\varepsilon>0$, where $M=M_{1} M_{2},|t| \geq 1$, and $0<\delta<1 / 52$. Then we have $$
L\left(\frac{1}{2}+i t, \pi \otimes \chi\right) \lll \pi, \varepsilon(M|t|)^{3 / 4-\delta+\varepsilon}
$$


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