

## LOWER CENTRAL WORDS IN FINITE $p$ -GROUPS

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**Abstract:** It is well known that the set of values of a lower central word in a group  $G$  need not be a subgroup. For a fixed lower central word  $\gamma_r$  and for  $p \geq 5$ , Guralnick showed that if  $G$  is a finite  $p$ -group such that the verbal subgroup  $\gamma_r(G)$  is abelian and 2-generator, then  $\gamma_r(G)$  consists only of  $\gamma_r$ -values. In this paper we extend this result, showing that the assumption that  $\gamma_r(G)$  is abelian can be dropped. Moreover, we show that the result remains true even if  $p=3$ . Finally, we prove that the analogous result for pro- $p$  groups is true.

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**Key words:**  $p$ -groups, commutators, lower central words.